

# Sedimentation of objects in aqueous foams.

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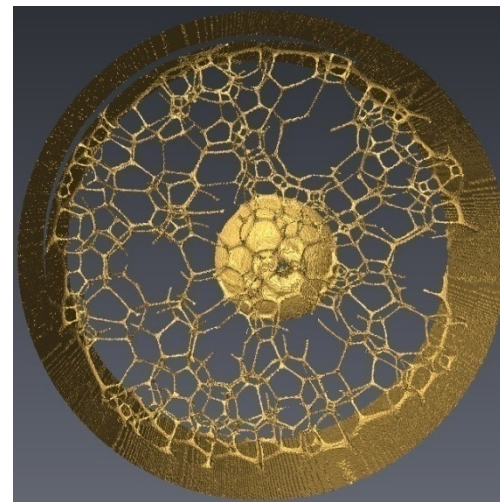
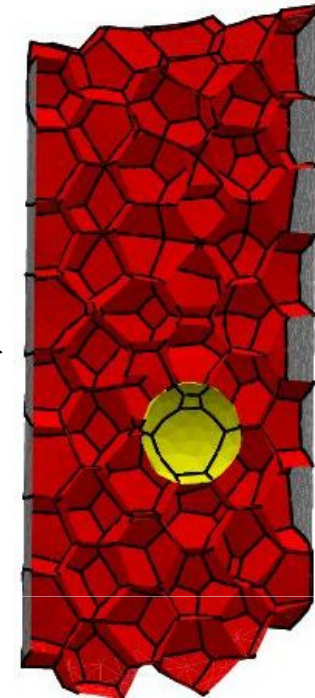
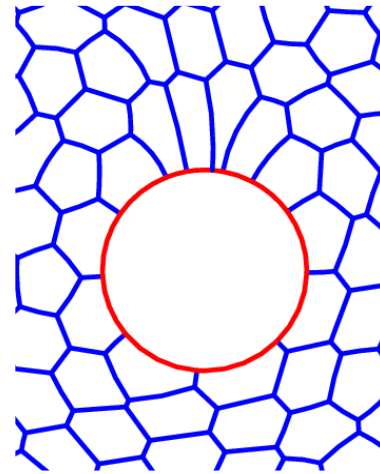
# Simulating Stokes' experiment in a foam

## 1. Two-dimensional

- Theory and visualization of the flow is simplified.
- Computational time is minimized.

## 2. Three-dimensional

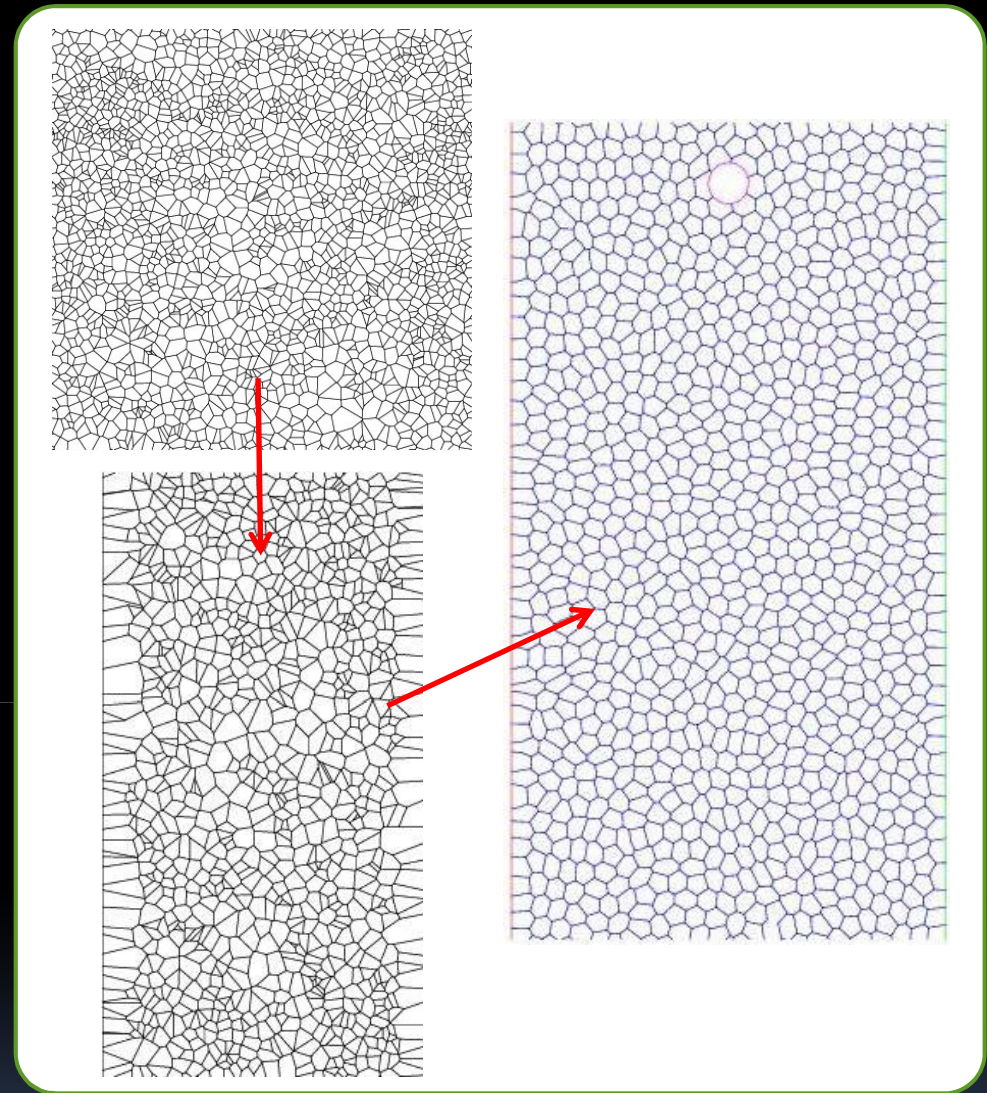
- More difficult to implement and visualize.
- To validate simulations we compare with experiments.



## 2D Simulations: Method

A structure that's topologically similar to a foam is built:

- Random **Voronoi** tessellation of the 2D unit square.
- Sequentially delete bubbles from either side and constrain outer edges to vertical walls.



### The **Surface Evolver**\*

minimizes the structure's *total edge length* subject to the bubble *area* constraints:

$$E = \gamma \sum_{\text{films } i} l_i + \sum_{\text{bubbles } k} p_k (A_k - A_k^t)$$

\*[www.susqu.edu/brakke/evolver](http://www.susqu.edu/brakke/evolver)

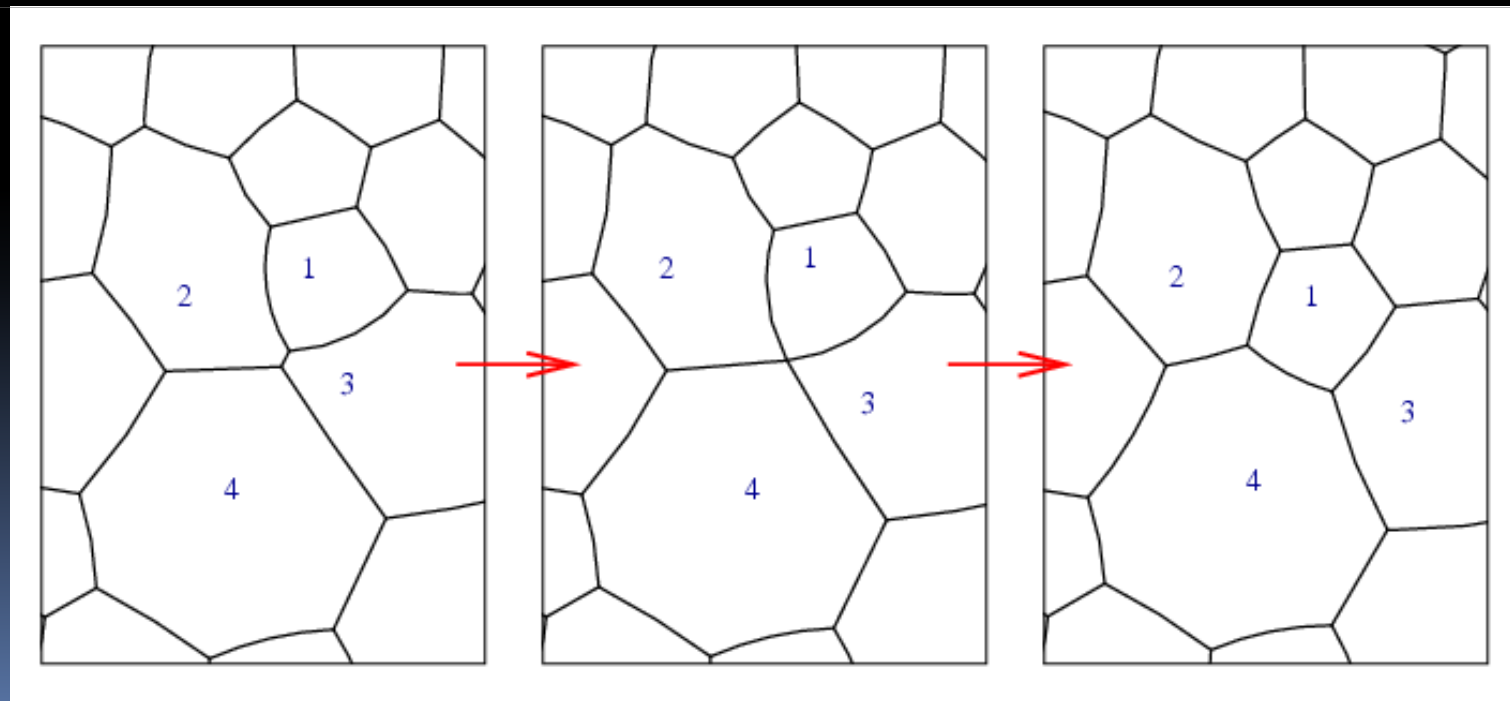
# T1 events in 2D Simulations

- Define a cut-off length  $l_c$ .
- Delete any edge that shrinks below this length.
- Insert a new edge in the perpendicular direction.

**Note:** The cut-off length relates to the effective liquid fraction:

$$\Phi_l \approx 0.242 \frac{l_c^2}{A_b}$$

*S. J. Cox et al. Rheol Acta, 43, 2004*



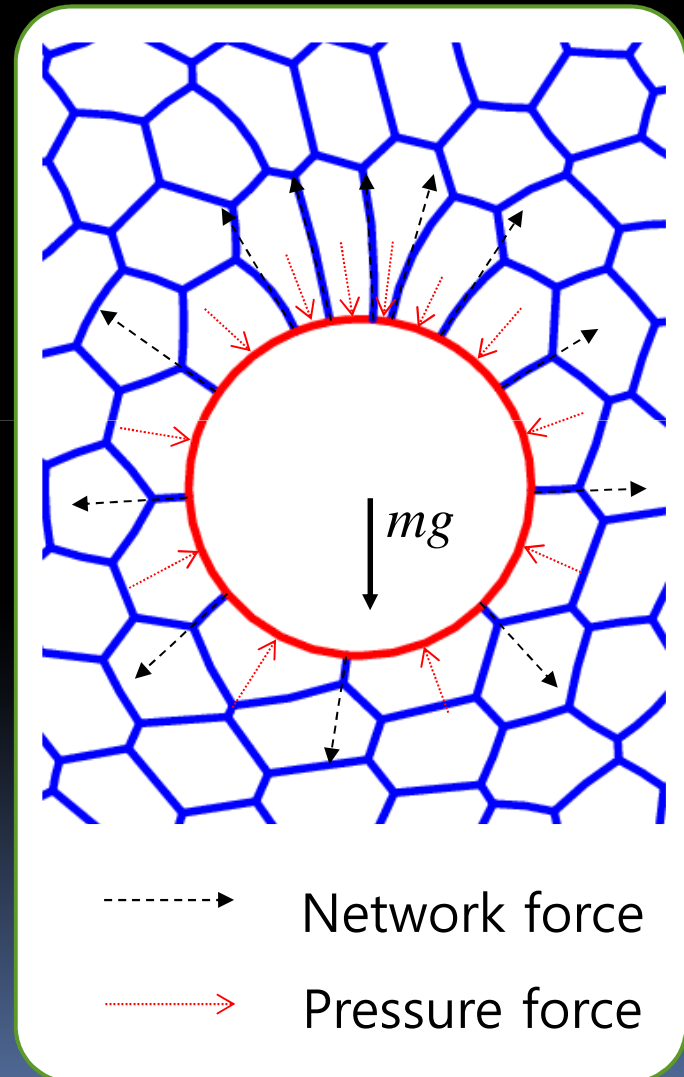
# Quasi-static model

- Motion of an object in a foam is governed by Newton's 2<sup>nd</sup> law of motion:

$$m \frac{d\vec{x}^2(t)}{dt^2} = mg\vec{z} - \lambda \frac{d\vec{x}(t)}{dt} + \vec{F}^p + \vec{F}^n$$

- We assume that the motion is **slow** and **steady**.
- The foam is in equilibrium between very small increments in the position of the object.
- A small constant epsilon ( $\epsilon=1/\lambda$ ) is chosen that sets the effective time scale of our simulation.

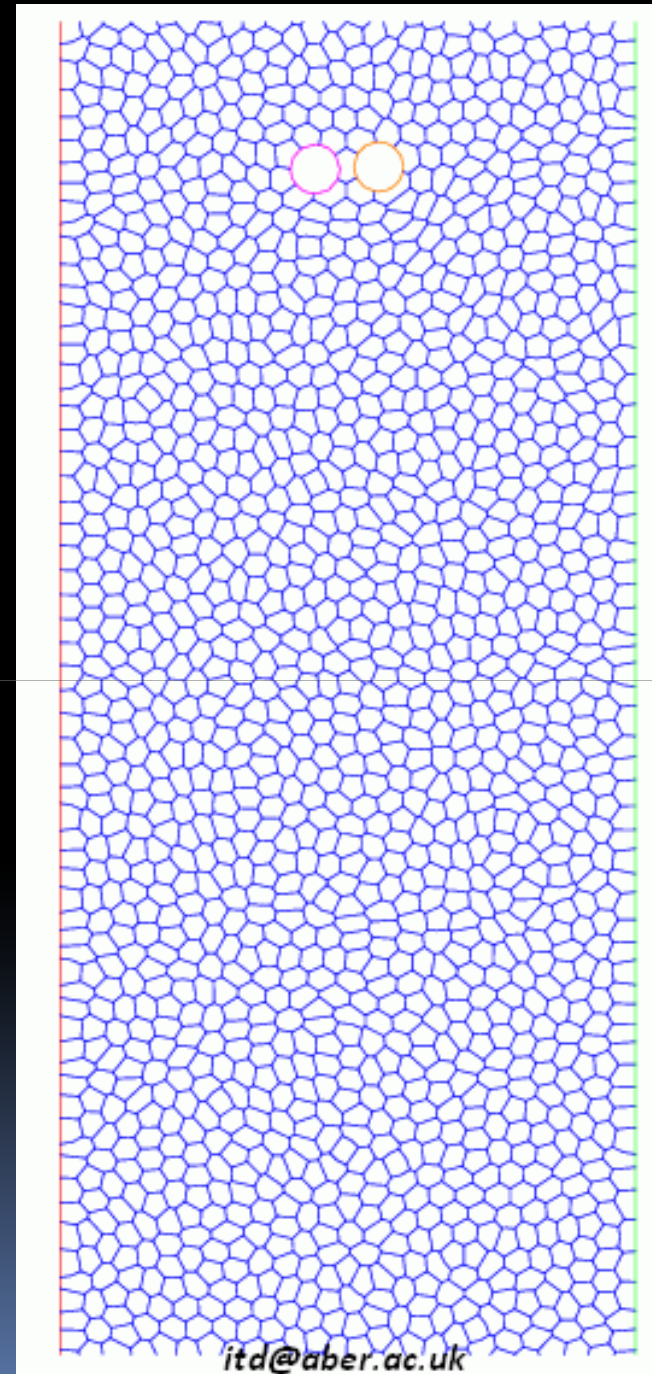
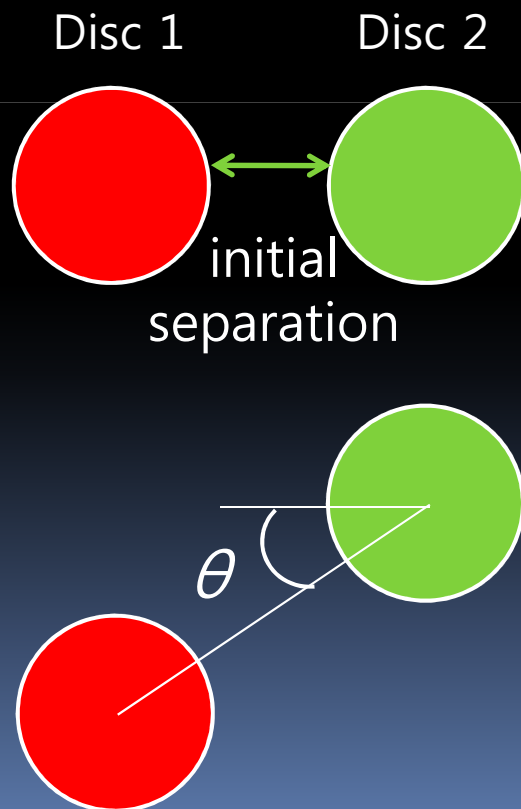
$$\frac{d\vec{x}(t)}{dt} = \epsilon (mg\vec{z} + \vec{F}^p + \vec{F}^n)$$





# Sedimentation of two circular discs:

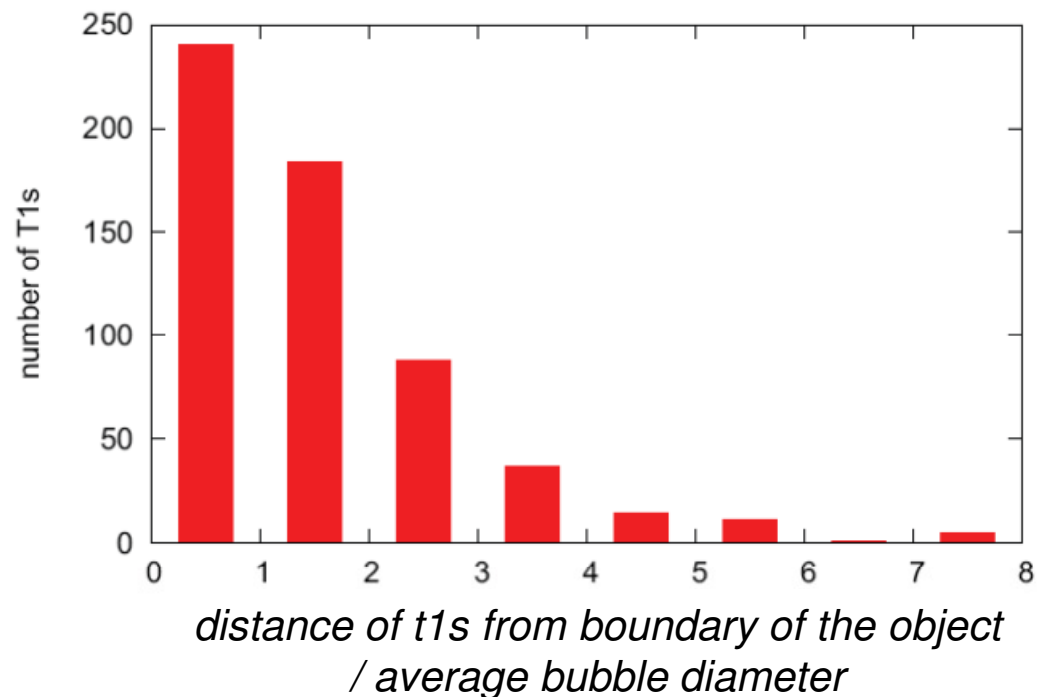
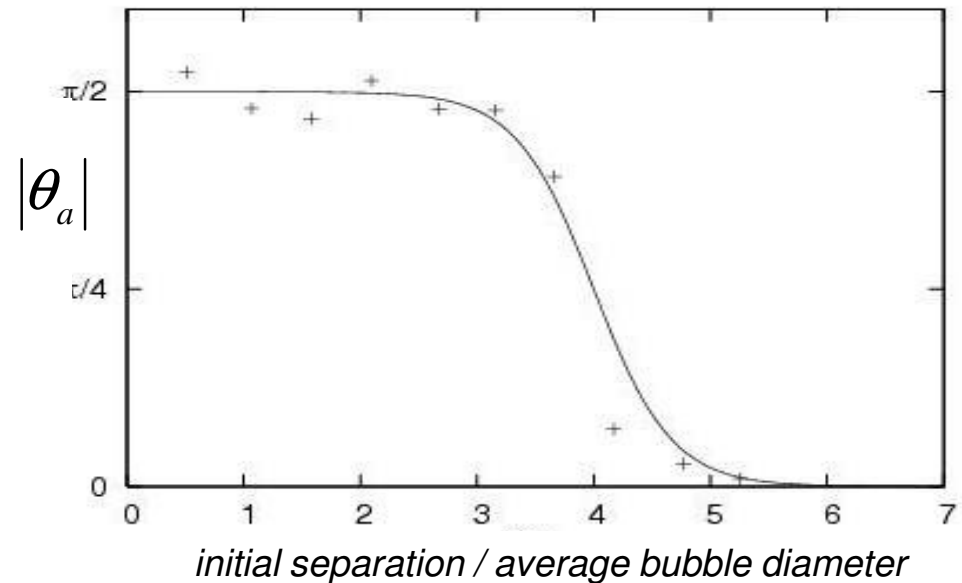
Discs interact by rotating about each other to a stable configuration as they sediment.



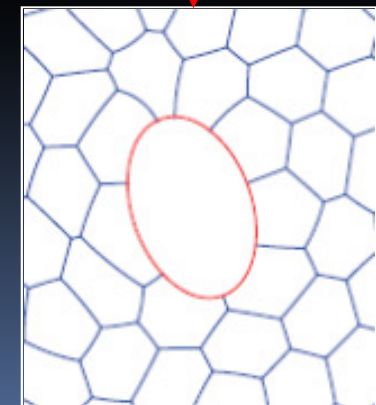
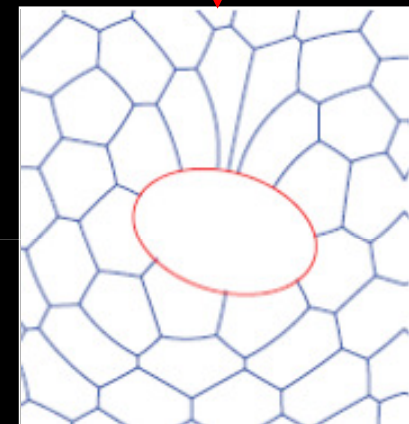
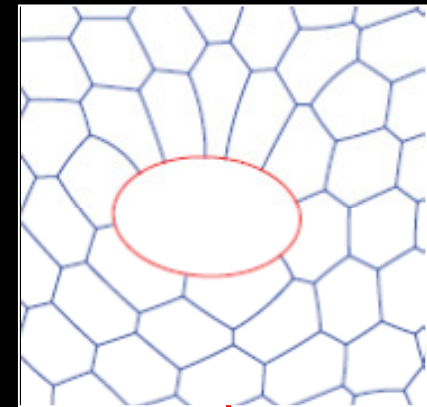
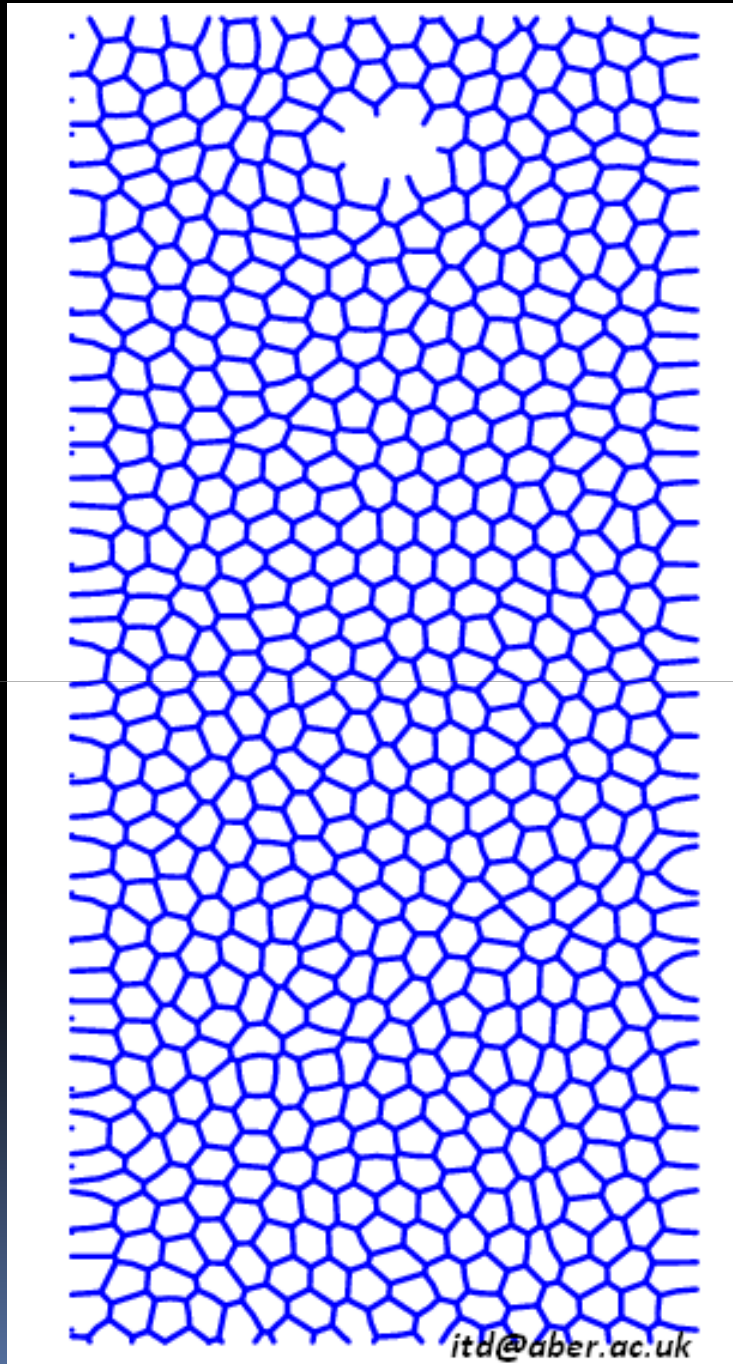
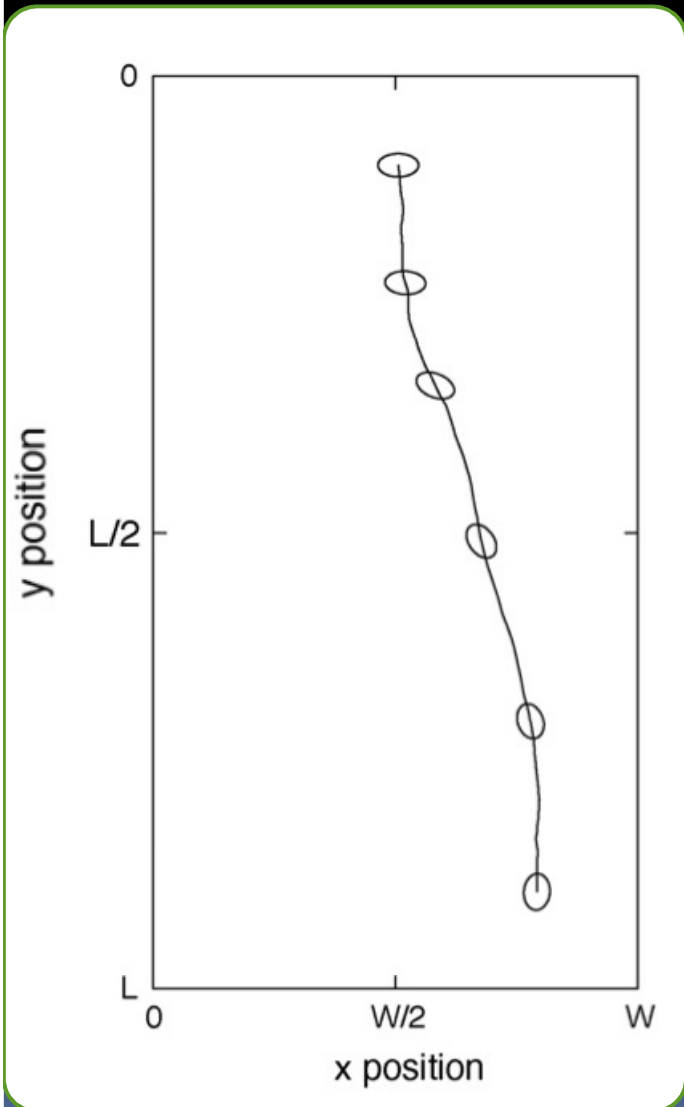
## Interaction between circular discs:

Let  $\theta_a$  denote the value of  $\theta$  at the bottom of the foam. The discs have fully interacted if  $|\theta_a| \approx \pi/2$ .

- A **critical separation** for disc-to-disc interaction exists due to the discrete nature of the foam.
- Objects interact in the foam if the **fluidized region** surrounding each object merge with each other.

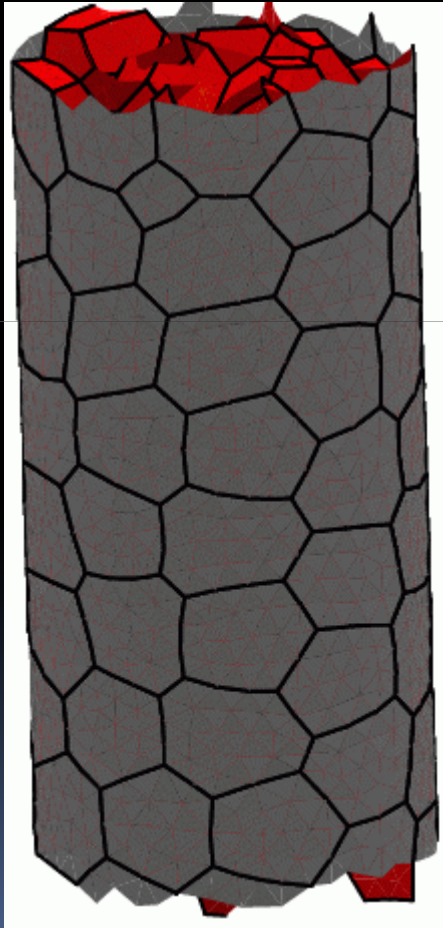


# Sedimenting Ellipse:





# 3D Simulations – Spheres in Disordered Foams

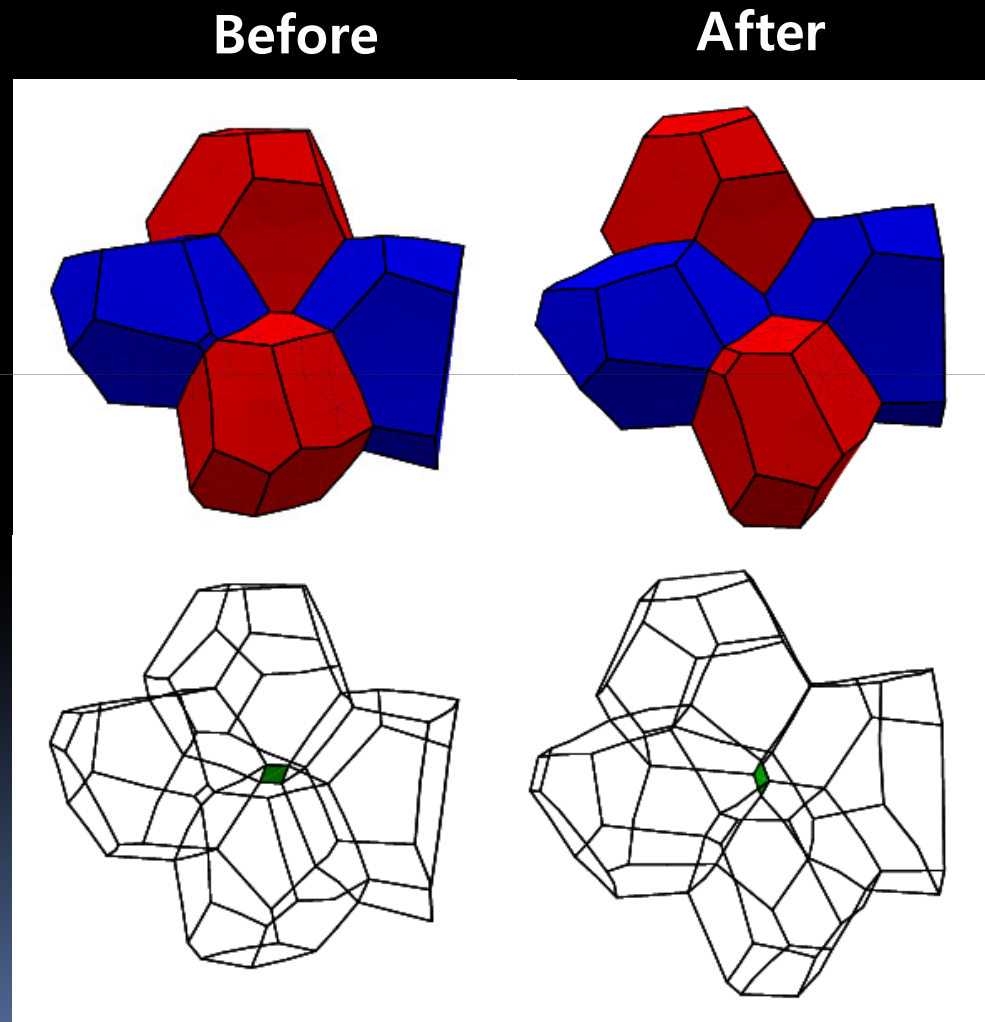


## New challenges:

- Building initial disordered structures that have minimal surface area.
- T1 events in 3D.
- Visualization of simulations is more complex.

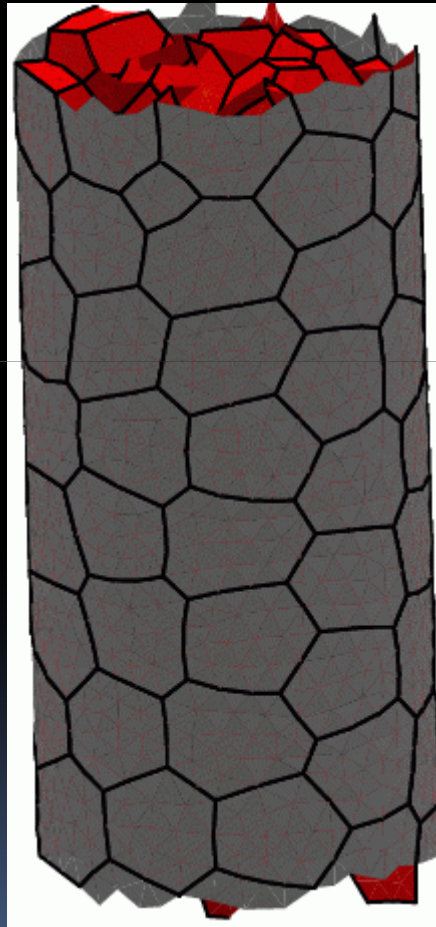
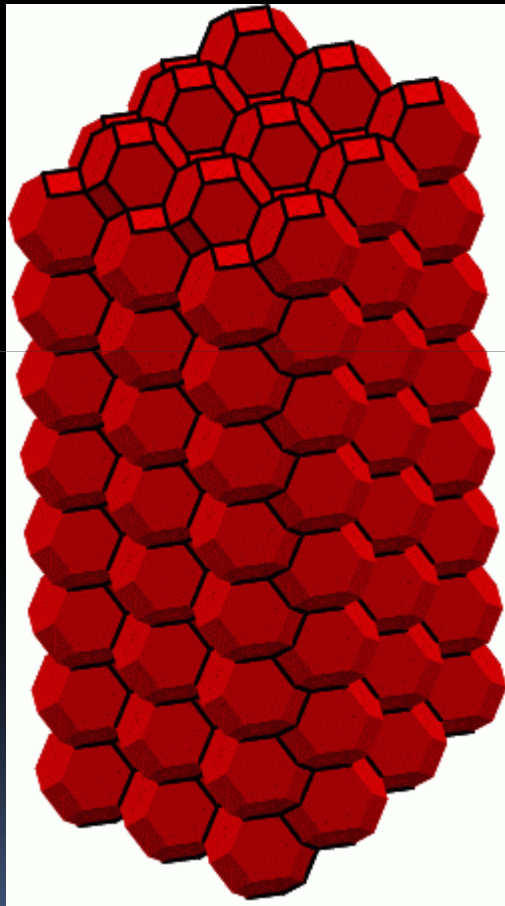
# T1 events in 3D simulations

- T1s are triggered when a facet shrinks below a predefined cut-off area  $a_c$
- Cut-off area defines the effective liquid fraction of the foam.
- We work with dry foams, where the liquid fraction  $\phi_l < 1\%$ .



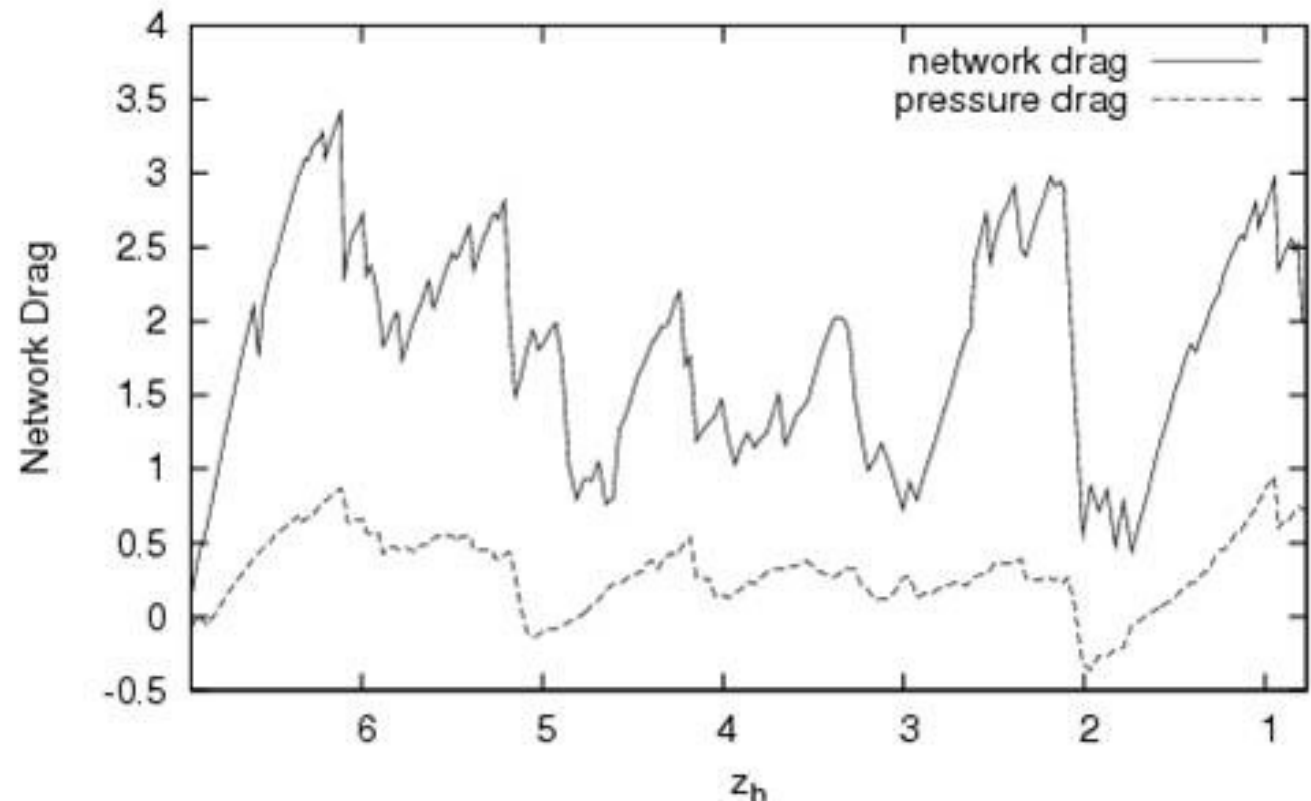
# 3D Simulations - Disordered Foams

Creation of the structure:



# Variation of the drag force on the sphere

- Network and pressure drag components fluctuate as
- bubbles detach and attach to the sphere due to t1s.
  - contacting bubble pressures varies due to the deformation caused by the sphere.



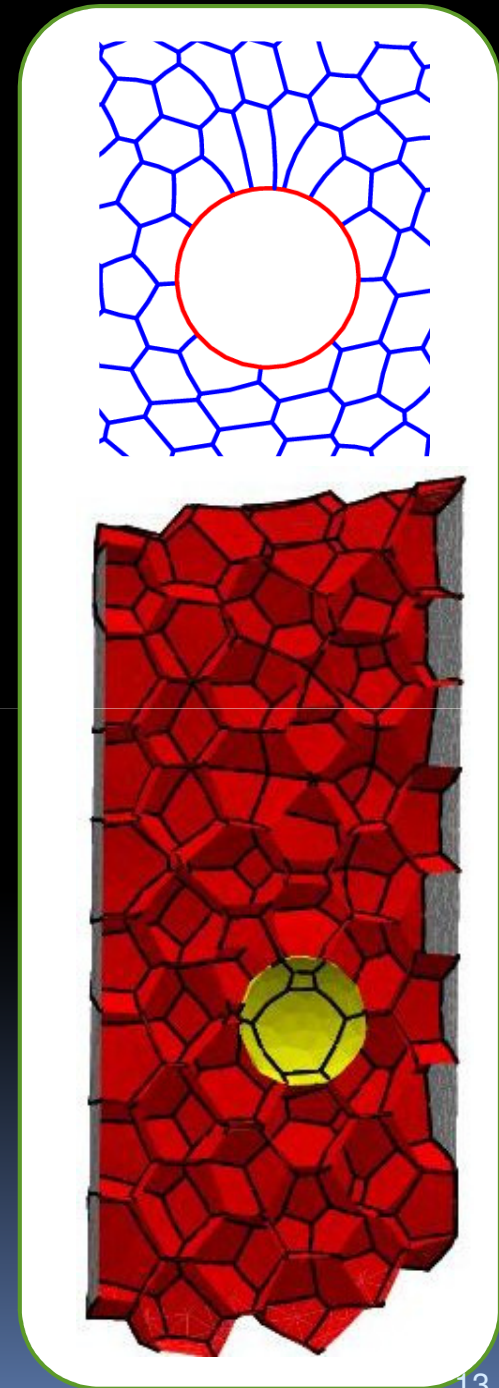


# Validation of Simulations

Our simulations need to be validated by comparing with experiment.

Limitations of the simulations to be investigate include

- the effect of **viscous dissipation**.
- the effect of **bubble volume dispersity**.
- variation of the **liquid fraction**.

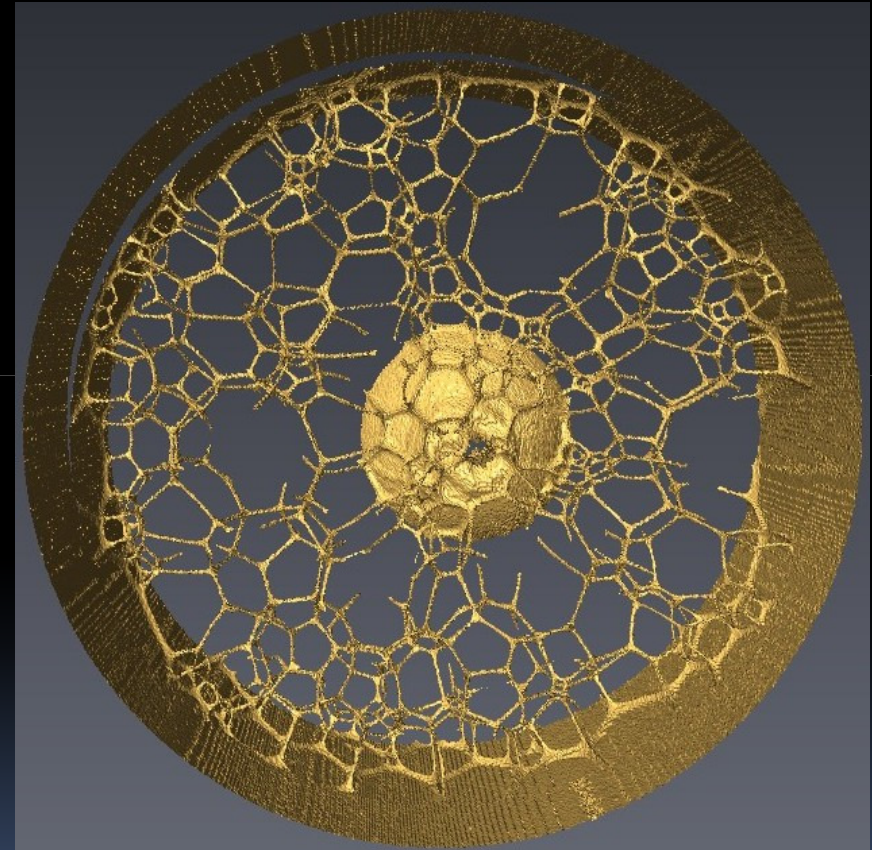




# Validation of Simulations

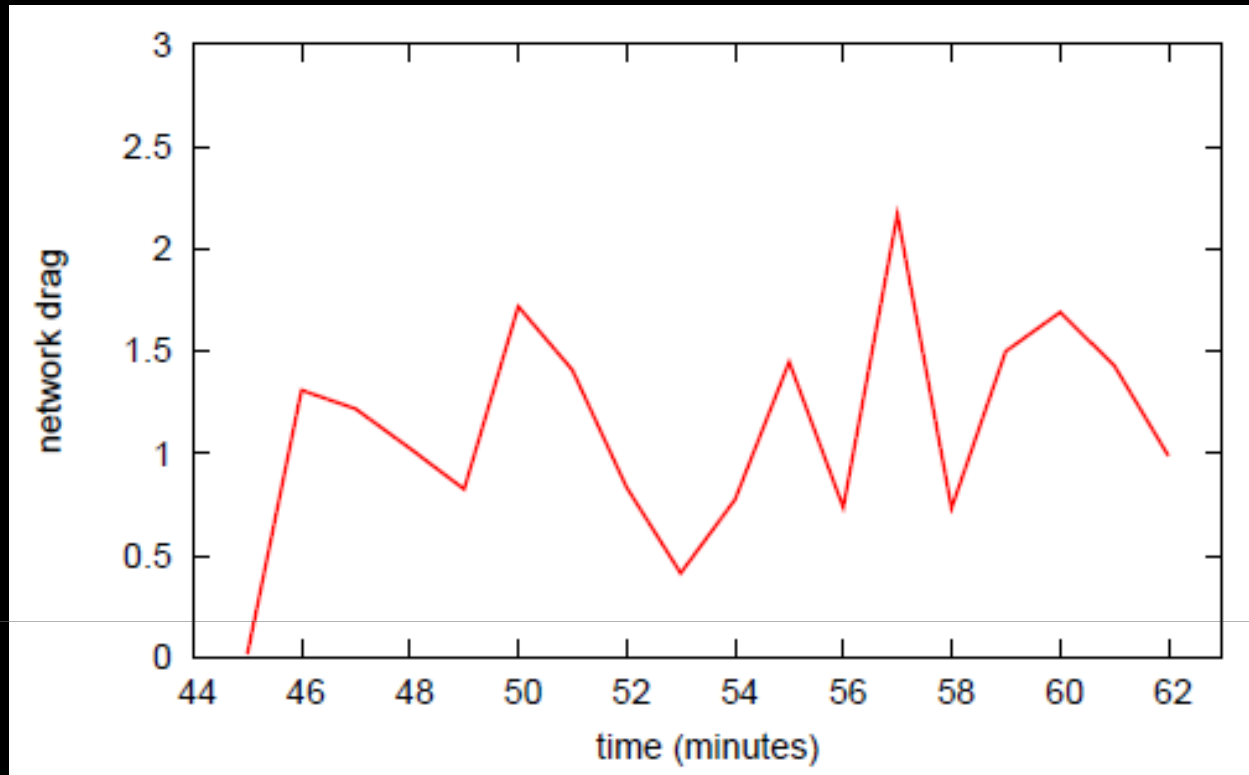
Data available of equivalent experiment obtained from X-ray tomography.

- **Films aren't observed.**
- A **partial reconstruction** of the foam can provide some validation for our simulations.
- e.g. Extracting the network of Plateau borders in contact with the sphere provides us with the **network force** exerted.



*J. Lambert et al, Coll. Surf. A. 263  
(2005)*

## Network force: 3D experiment



- Foam is dry as in simulation (liquid fraction is less than 3%).
- Flow is very slow – quasistatic approximation is appropriate.

## Summary / Conclusions

- Progress in going from 2D to 3D simulations.
- 3D simulations of disordered foams are more challenging.
- Reconstruction of 3D disordered foams is required to validate.
- Only a partial reconstruction of the foam is required for calculation of the network force.